

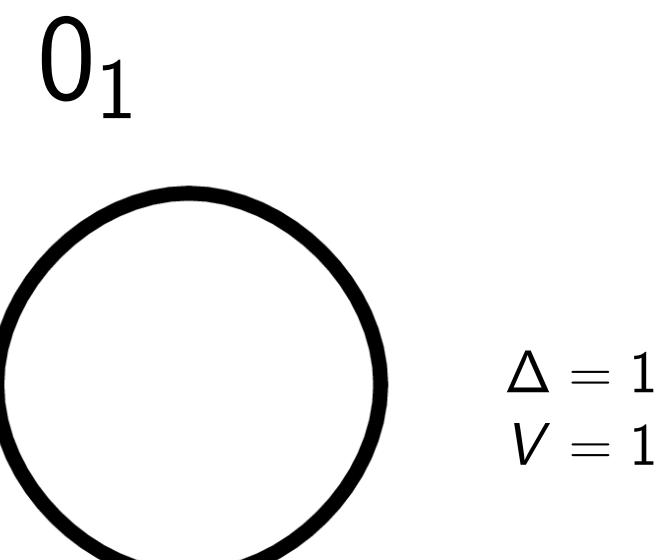


In matematica

Un *nodo* è una curva chiusa nello spazio. Possiamo pensare ad un intreccio di una corda, i cui estremi sono stati incollati. Attraverso un disegno nel piano con alcuni incroci possiamo facilmente descrivere un nodo.

Unknot

L'esempio più semplice è quello di un nodo in cui l'intreccio è sciolto: il *nodo banale*.

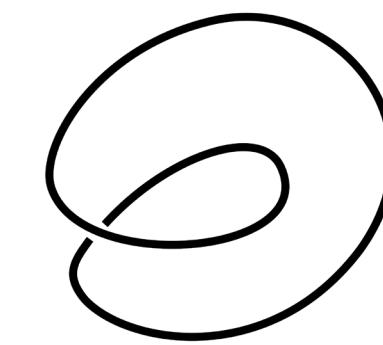


$$\Delta = 1 \\ V = 1$$

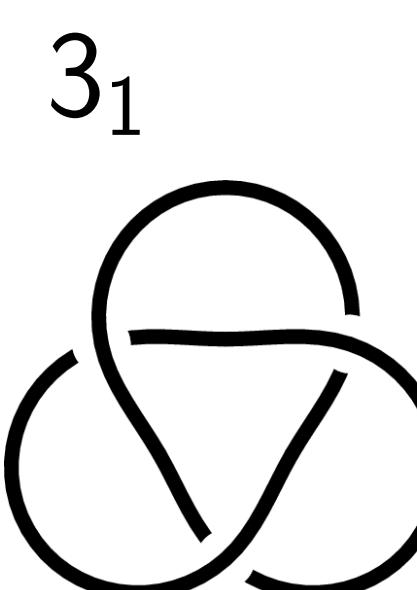
Nodi equivalenti

Due nodi si dicono *equivalenti* se possono essere ottenuti l'uno dall'altro attraverso alcune mosse elementari. Capire quando due diagrammi identificano lo stesso nodo non è così semplice.

Ad esempio, lo diresti che questo è un nodo banale?

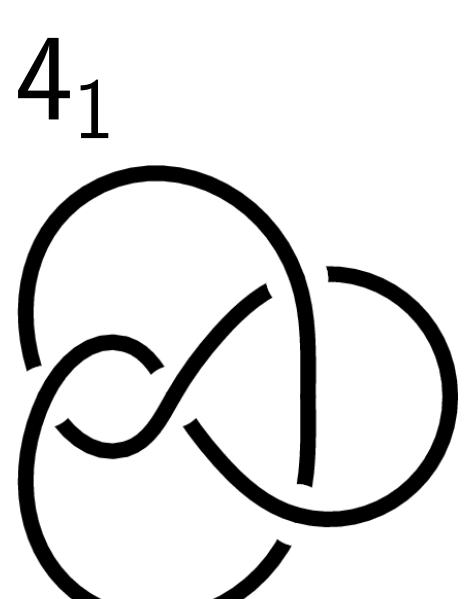


Il nodo trifoglio

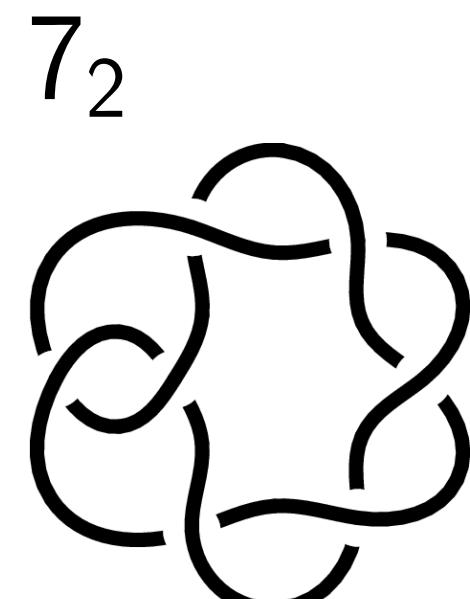


$$\Delta = 1 - t + t^2 \\ V = -q^{-4} + q^{-3} + q^{-1}$$

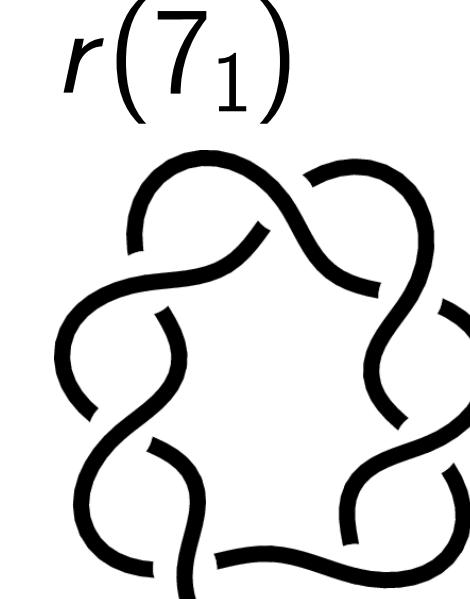
Indovina il nodo!



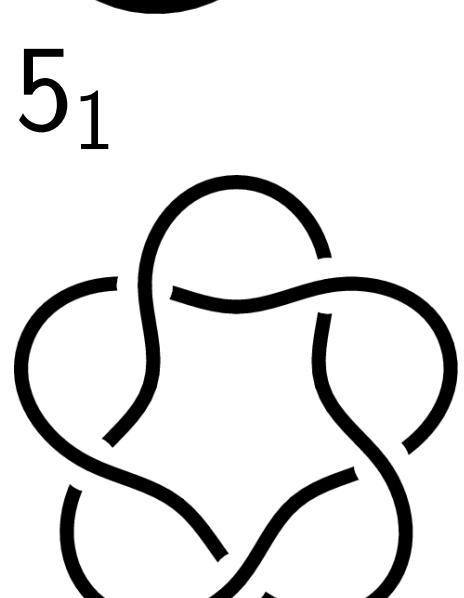
$$\Delta = 1 - 3t + t^2 \\ V = q^{-2} - q^{-1} + 1 - q + q^2$$



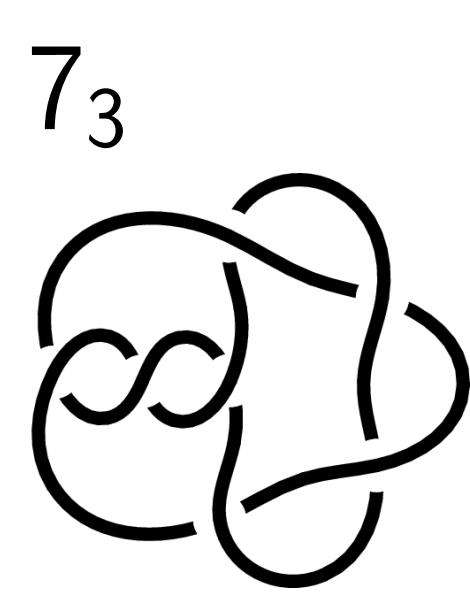
$$\Delta = 3 - 5t + 3t^2 \\ V = -q^{-8} + q^{-7} - q^{-6} + 2q^{-5} \\ -2q^{-4} + 2q^{-3} - q^{-2} + q^{-1}$$



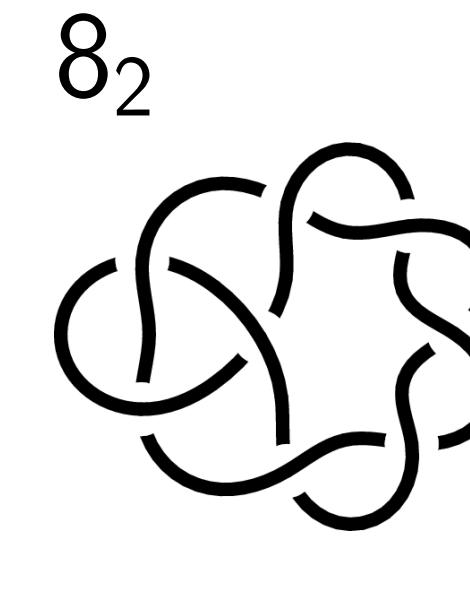
$$\Delta = 1 - t + t^2 - t^3 + t^4 - t^5 + t^6 \\ V = q^3 + q^5 - q^6 + q^7 - q^8 \\ +q^9 - q^{10}$$



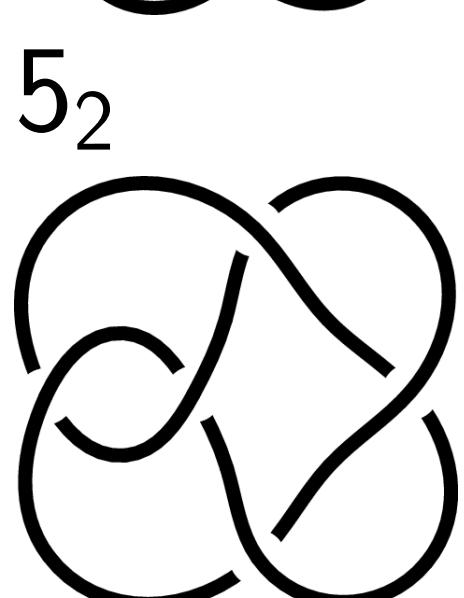
$$\Delta = 1 - t + t^2 - t^3 + t^4 \\ V = -q^{-7} + q^{-6} - q^{-5} + q^{-4} + q^{-2}$$



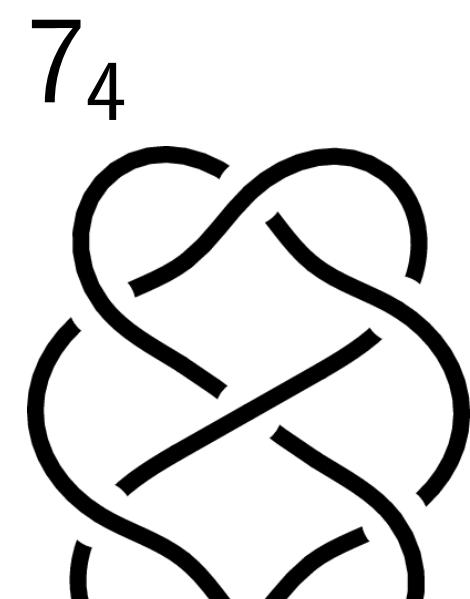
$$\Delta = 2 - 3t + 3t^2 - 3t^3 + 2t^4 \\ V = -q^9 + q^8 - 2q^7 + 3q^6 - 2q^5 \\ +2q^4 - q^3 + q^2$$



$$\Delta = 1 - 3t + 3t^2 - 3t^3 + 3t^4 \\ -3t^5 + t^6 \\ V = 1 - q^{-1} + 2q^{-2} - 2q^{-3} + 3q^{-4} \\ -3q^{-5} + 2q^{-6} - 2q^{-7} + q^{-8}$$



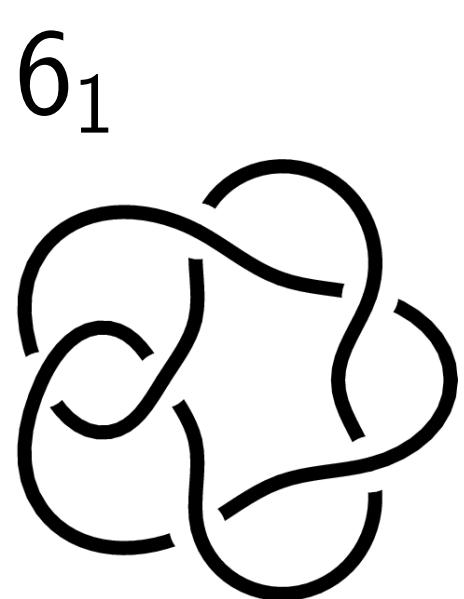
$$\Delta = 2 - 3t + 2t^2 \\ V = -q^{-6} + q^{-5} - q^{-4} + 2q^{-3} \\ -q^{-2} + q^{-1}$$



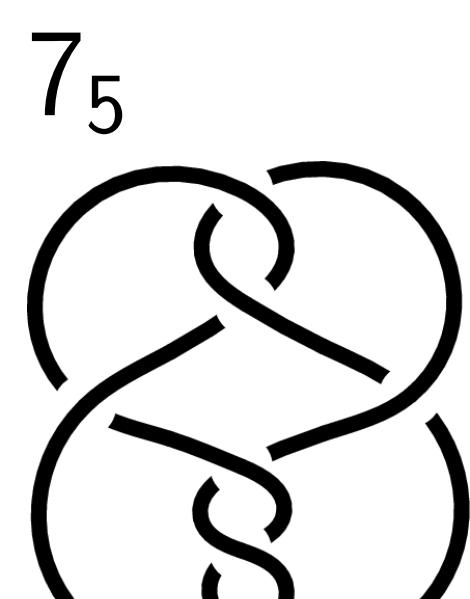
$$\Delta = 4 - 7t + 4t^2 \\ V = -q^8 + q^7 - 2q^6 + 3q^5 - 2q^4 \\ +3q^3 - 2q^2 + q$$



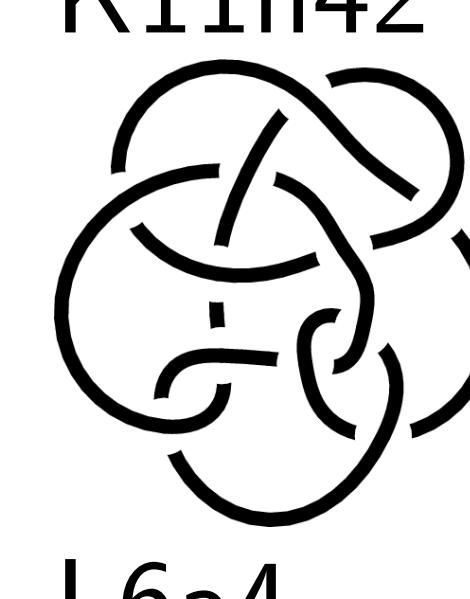
$$\Delta = 1 \\ V = -q^4 + 2q^3 - 2q^2 + 2q + q^{-2} \\ -2q^{-3} + 2q^{-4} - 2q^{-5} + q^{-6}$$



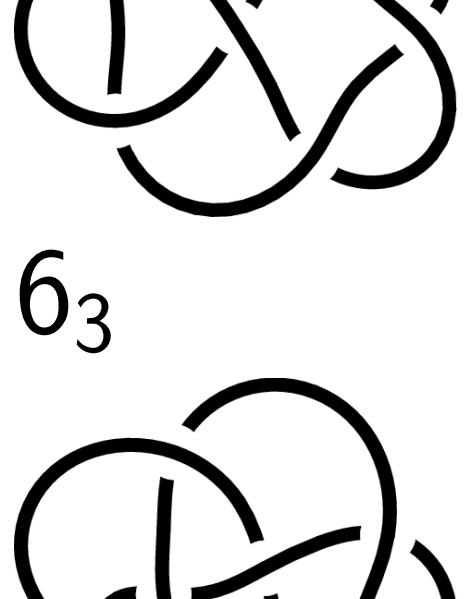
$$\Delta = -2 + 5t - 2t^2 \\ V = q^2 - q + 2 - 2q^{-1} + q^{-2} \\ -q^{-3} + q^{-4}$$



$$\Delta = 2 - 4t + 5t^2 - 4t^3 + 2t^4 \\ V = -q^{-9} + 2q^{-8} - 3q^{-7} + 3q^{-6} \\ -3q^{-5} + 3q^{-4} - q^{-3} + q^{-2}$$



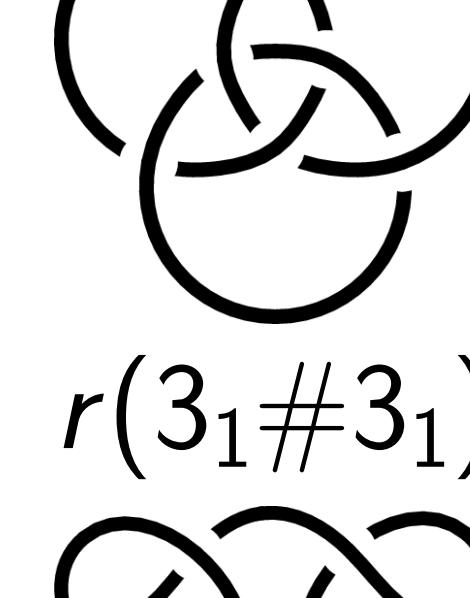
$$\Delta = 1 \\ V = -q^4 + 2q^3 - 2q^2 + 2q + q^{-2} \\ -2q^{-3} + 2q^{-4} - 2q^{-5} + q^{-6}$$



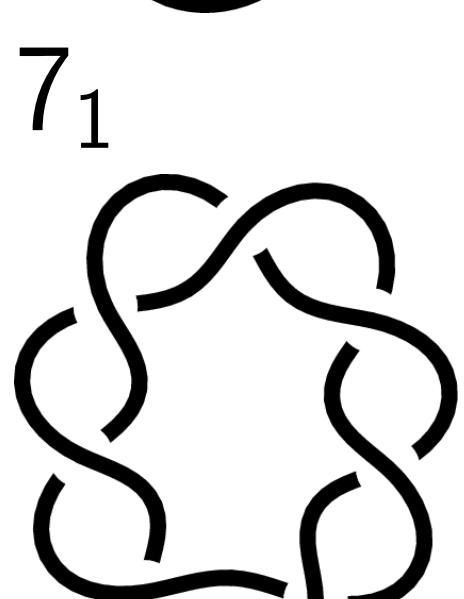
$$\Delta = 1 - 3t + 3t^2 - 3t^3 + t^4 \\ V = q - 1 + 2q^{-1} - 2q^{-2} + 2q^{-3} \\ -2q^{-4} + q^{-5}$$



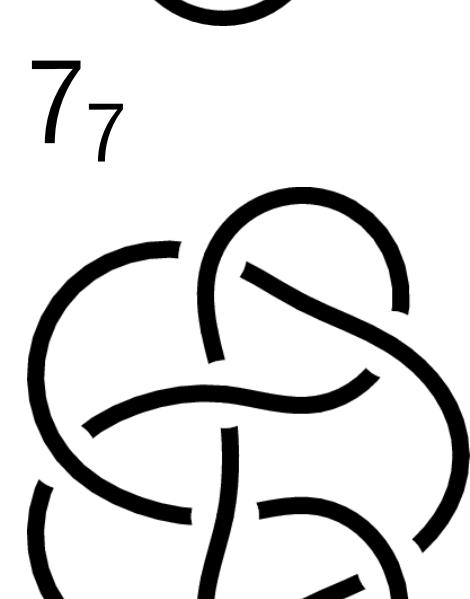
$$\Delta = 1 - 5t + 7t^2 - 5t^3 + t^4 \\ V = q - 2 + 3q^{-1} - 3q^{-2} + 4q^{-3} \\ -3q^{-4} + 2q^{-5} - q^{-6}$$



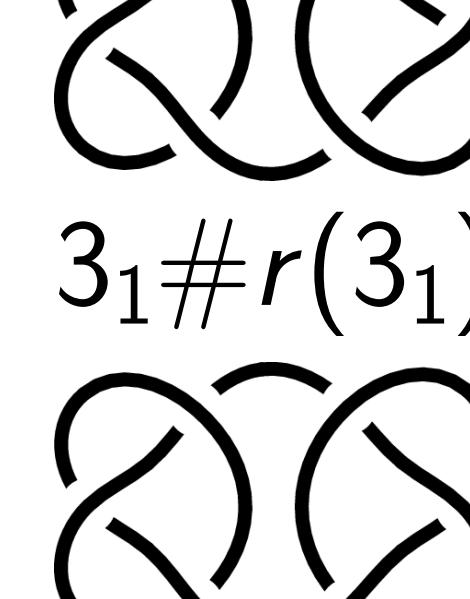
$$\Delta = (u - 1)(v - 1)(w - 1) \\ V = -q^3 + q^{-3} + 3q^2 + 3q^{-2} - 2q^{-1} + 4$$



$$\Delta = 1 - 3t + 5t^2 - 3t^3 + t^4 \\ V = -q^3 + 2q^2 - 2q + 3 - 2q^{-1} \\ +2q^{-2} - q^{-3}$$



$$\Delta = 1 - 5t + 9t^2 - 5t^3 + t^4 \\ V = q^4 - 2q^3 - q^{-3} + 3q^2 + 3q^{-2} \\ -4q - 3q^{-1} + 4$$



$$\Delta = (1 - t + t^2)^2 \\ V = (q + q^3 - q^4)(-q^{-4} + q^{-3} + q^{-1})$$